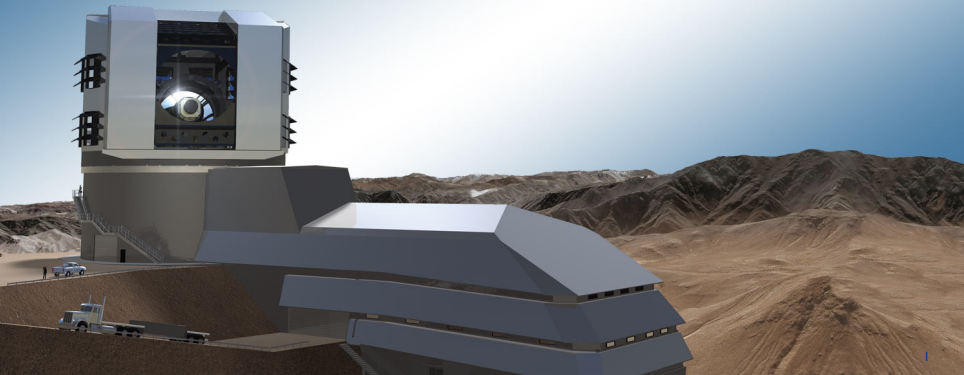


Flatfielding a Widefield Camera

Robert Lupton, Mario Jurić, and Christopher Stubbs

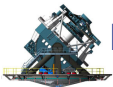
2014-12-04





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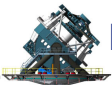
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We need to find

$$C_{std,b} \equiv \int_0^\infty F_\nu S_{std,b} d\lambda / \lambda$$

given $C_{raw,b}$ (where $S_{std,b}$ is some average $S^{atm} S_b^{sys}$).



Measuring $C_{std,b}$

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- Estimate the instrumental sensitivity $S_b^{sys}(\lambda)$



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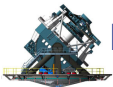


Input Datasets



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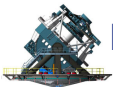
-- Broad-band flats



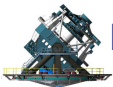
- Broad-band flats
- "Monochromatic" (c. 1 nm bandwidth) flats, calibrated with NIST photodiodes observing the calibration screen.



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- A collimated "monochromatic" projector
- Atmospheric Stuff (a 1.2m telescope with $R \sim 300 - 400$ spectrophotometry; two units to measure water vapour; a commercial all-sky monitor using GPS satellites and a bore-sight mounted radiometer to measure the profile)



The instrumental sensitivity $S_b^{\text{sys}}(\lambda, \mathbf{x})$



Let $\mathcal{I}(\lambda, \mathbf{x})$ be the illumination of the focal plane due to the illuminated flatfield screen in the absence of telescope and filter effects and $\mathcal{F}_b(\lambda, \mathbf{i})$ the flatfield image.



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Unfortunately, \mathcal{F}_b also includes scattered light and ghosting:

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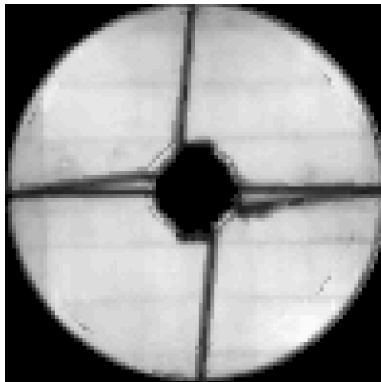
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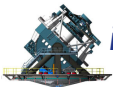
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N.b. We wrote S_b not S_b^{sys} because there are multiplicative effects other than quantum efficiency that enter into \mathcal{F}_b (e.g. pixel size variations).

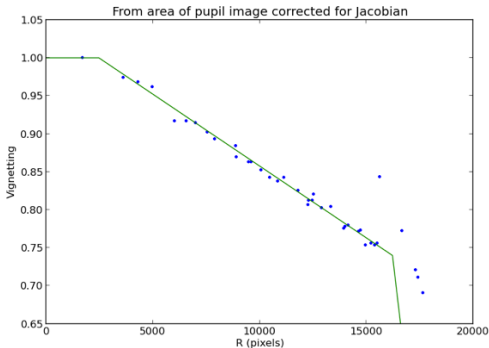


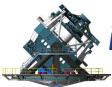
$i(\lambda, \mathbf{i})$ and vignetting in HSC



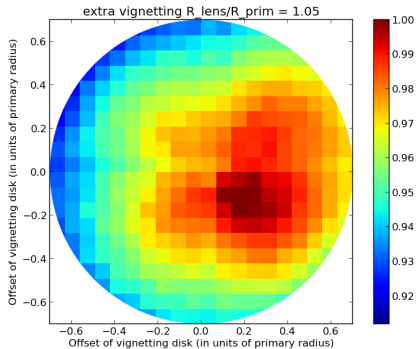


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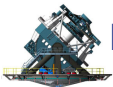
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Structures seen in S_b can come from either QE variations in the system and vignetting, or changes in the effective size of the pixels:

$$S_b(\lambda, \mathbf{i}) = S_b^{filt}(\lambda, \mathbf{i}) \times S^{tel}(\lambda, \mathbf{i}) \times S^{vig}(\lambda, \mathbf{i}) \times S^{qe}(\lambda, \mathbf{i}) \times S^{geom}(\lambda, \mathbf{i})$$



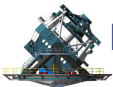
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For measures of surface brightness QE/vignetting and geometrical effects are equivalent, but for measurements of objects' fluxes we must be careful to separate them; treating larger pixels as more sensitive can give incorrect results.



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We plan to use star flats as a cross-check, not a primary measurement.



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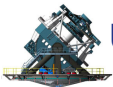
The projector will also generate a series of ghosts, but only a small portion of the pupil is illuminated.



Using the Collimated Projector

We need to allow for only illuminating a portion of the pupil. If we label the spots by ℓ , a single spot's flux is

$$P_b^\ell(\lambda, \mathbf{x}_i, \mathbf{X}) = a^\ell I(\lambda) (1 + i(\lambda)) S_b^{\text{filt}}(\lambda) S^{\text{tel, qe, vig, optics, ccd}}(\lambda)$$



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so after scanning the projector over the pupil, we have

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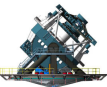
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If we now move these spots around the LSST focal plane, taking data at only a single position in the pupil and wavelength, we may solve for the spots' relative amplitudes.



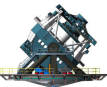
Once we know the d^ℓ 's, we scale all the spot intensities to a common scale,

$$P_b^\ell(\mathbf{x}_i) = I S^{qe, optics, ccd} \int_{pupil} (1 + i) S_b^{filt} S^{tel, vig} d\mathbf{x}$$

and

$$\mathcal{F}_b(\lambda, \mathbf{x}_i) = P_b^\ell(\mathbf{x}_i) + I S^{qe, optics, ccd} \int_{pupil} \mathcal{A}_b S_b^{filt} S^{tel, vig} d\mathbf{x}$$

If the first term varies only slowly over a chip, then rastering the spots to illuminate e.g. 9 positions on each chip allows us to evaluate $P_b^\ell(\mathbf{i})$, i.e. at every pixel.



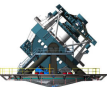
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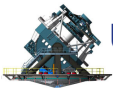
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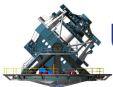
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For many cameras the spatial structure of \mathcal{A} has sharp features. Furthermore, the operations described above are expensive, and we have to repeat for every 1nm step in wavelength. If we know the filter bandpasses $S_b^{filt}(\mathbf{i})$ at every point in the focal plane we may use a slightly different approach.



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- there are no strongly chromatic elements so we can use larger steps in wavelength
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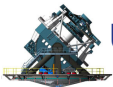


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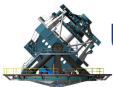
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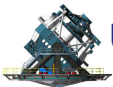
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There's only one remaining contaminant: the non-uniform illumination resulting from an imperfect flatfield screen, i .



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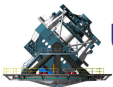
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There's only one remaining contaminant: the non-uniform illumination resulting from an imperfect flatfield screen, i .

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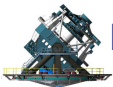


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By interpolating and then summing over the focal plane we have an estimate of \mathcal{A}_b ; it will be interesting to see how well this works.



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- it does not remove the need for sufficiently scrupulous algorithms to require access to the per-pixel geometrical information.



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This is the flatfield that best flattens the sky once warped onto a tangent plane, at the cost of photometric errors.



The object's SED

Let us remember that we don't actually need to know the SED; we need merely to know enough about it to allow us to make sufficiently accurate corrections from $C_{raw,b}$ to $C_{std,b}$.



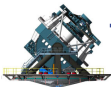
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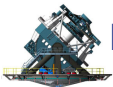
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There is nothing we can do about this degeneracy, which means that we cannot hope to correctly estimate C_b^{std} for a subset of objects which we detect. We shall define a deterministic mapping from colour to SED $(\{C_b\}, \theta)$ which will allow a consumer of the data to make their own correction.



Measuring the background level

We plan to background match exposures before sky subtraction, generating a stacked image in a sky projection. This results in two data products:

- The background image in the stacked image B^{stack} .
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If we had included S^{ccd} in the flatfield we would have handled the background correctly if we also included it in the warps to and from sky coordinates, but we would not be able to forget about it as it continues to have effects on the astrometry and photometry.



Background Subtracted Images

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- We could decide to now correct for S^{ccd} .



The signal that we measure after (incorrectly) flat fielding with a flat constructed using the sky's SED is

$$I_j = a \int_b S_{obj}^{atm} \frac{S_{b,j,obj}^{filt} S_{j,obj}^{tel} S_{j,obj}^{qe}}{S_{b,j,sky}^{filt} S_{j,sky}^{tel} S_{j,sky}^{qe}} S_j^{ccd} M_j P_b(\lambda) d\lambda + \epsilon_j \equiv aw_j + \epsilon_j$$

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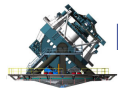


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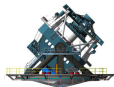
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and, correcting to a standard atmosphere, and writing $w = S_j^{ccd} M_j$

$$C_{std} = \frac{S_{obj,std}^{atm}}{S_{obj}^{atm}} \frac{S_{b,sky}^{filt} S_{sky}^{qe}}{S_{b,obj}^{filt} S_{obj}^{qe}} \frac{\sum_j w_j I_j \sum_j w_j}{\sum_j (w_j)^2}$$

$$\equiv \frac{S_{obj,std}^{atm}}{S_{obj}^{atm}} \frac{S_{b,sky}^{filt} S_{sky}^{qe}}{S_{b,obj}^{filt} S_{obj}^{qe}} C_{raw}$$

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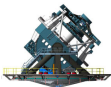


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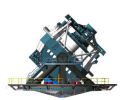
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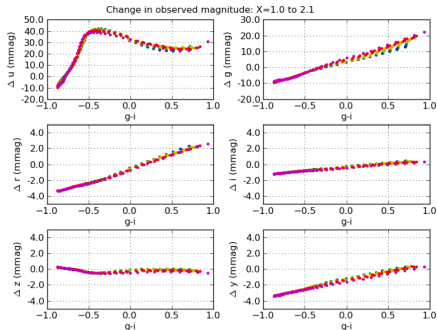
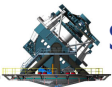
Note that the SED doesn't enter into the pixel-dependent part, C_{raw}^r , making it relatively simple to adopt a different SED and recalculate C_{std} if we know the c_{SED}^r . This relies depends on our assumption about the constancy of $S_{obj}^{tel}/S_{sky}^{tel}$ and $S_{obj}^{qe}/S_{sky}^{qe}$ over the object.



Because we use a model-based approach to handle SED dependencies we can easily handle more complicated problems; for example, if we are using a bulge/disk decomposition we are estimating the colours of each component, and can handle their SEDs separately when fitting our model.



The End



The change in observed magnitudes due to changes in airmass from $X = 1.0$ to $X = 2.1$, for a typical atmospheric transmission response curve.



We will have many-colour photometry (*ugrizy*) of many, many stars in each visit. We know from simulations of Kurucz models that as the properties of the atmosphere are varied there are several percent level changes in fluxes, with percent-level scatter at a given $g - i$ colour. It is not yet clear how much of this scatter can be regressed out using all five available colours.

Even if the scatter can be removed to SRD precision it is not clear how well we will be able to characterize S^{atm} across the filter b .



Even if the photometry is unable to constrain S^{atm} well enough to satisfy the SRD requirements, it seems very likely that we will be able to say something interesting. Once we have implemented an initial version of the photometric analysis we will be able to analyse wide-field camera data to explore the structure functions.